

1 **Spectral resampling based on user-defined inter-band correlation filter: C₃**
2 **and C₄ grass species classification**

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5 Clement Adjorlolo^{a*}, Onesimo Mutanga^a, Moses A. Cho^{a,b}, Riyad Ismail^a

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7
8 ^aUniversity of KwaZulu-Natal, School of Agriculture, Earth and Environmental Sciences, P. Bag X01,
9 Scottsville 3209, Pietermaritzburg, South Africa

10 ^bCouncil for Industrial and Scientific Research, Meiring Naude Road, P.O. Box 395, Pretoria 0001, South Africa

11 *Corresponding author. Email: clement.adjorlolo@kzndae.gov.za

12
13 **Abstract**

14 In this paper, a user-defined inter-band correlation filter function was used to resample
15 hyperspectral data and thereby mitigate the problem of multicollinearity in classification
16 analysis. The proposed resampling technique convolves the spectral dependence information
17 between a chosen band-centre and its shorter and longer wavelength neighbours. Weighting
18 threshold of inter-band correlation (WTC, Pearson's r) was calculated, whereby $r = 1$ at the
19 band-centre. Various WTC ($r = 0.99$, $r = 0.95$ and $r = 0.90$) were assessed, and bands with
20 coefficients beyond a chosen threshold were assigned $r = 0$. The resultant data were used in
21 the random forest analysis to classify C₃ and C₄ grass species. The respective WTC datasets
22 yielded improved classification accuracies (kappa = 0.82, 0.79 and 0.76) with less correlated
23 wavebands when compared to resampled Hyperion bands (kappa = 0.76). Overall, the results
24 obtained from this study suggested that resampling of hyperspectral data should account for
25 the spectral dependence information to improve overall classification accuracy as well as
26 reducing the problem of multicollinearity.

27
28 **Keywords:** Spectral resampling; Inter-band correlation; Grass species classification; Random
29 forests

1

2 **1. Introduction**

3 Discriminating grass species, which correspond to the 3-carbon (C_3) or 4-carbon (C_4)
4 photosynthetic pathways, is consistent with the plant functional type (PFT) approach used in
5 land surface modelling schemes (Tieszen et al., 1997; Ustin and Gamon, 2010). In general,
6 C_3 and C_4 grasses differ significantly in a number of physiological and anatomical
7 characteristic features. The C_4 type of grass species has more compact leaf mesophyll, higher
8 proportion of vascular tissue and a lower interveinal distance, than those of C_3 grasses. In
9 addition, several biochemicals such as intercellular air-moisture and nitrogen concentration
10 are relatively lower in C_4 grass, compared to C_3 grass species (Oyarzabal et al., 2008). Such
11 differences can manifest in the composition of C_3 and C_4 grasslands, with the dominant
12 species strongly constituting the canopy reflectance. The fundamental principle is that C_3 and
13 C_4 grass canopy reflectance is directly dependent on their spectral properties, which are in
14 turn, controlled by the biophysical and biochemical characteristics of vegetation (Mutanga et
15 al., 2004). Several empirical evidences have shown that the spectral variability between C_3
16 and C_4 grass species or groups of grasses is greater than the within group spectral information
17 (Irisarri et al., 2009; Liu and Cheng, 2011; Smith and Blackshaw, 2003). For example,
18 reflectance at 531 and 570 nm have been proposed as a set of spectral bands sensitive to
19 differences in C_3 and C_4 species (Gamon et al., 1997). Slaton et al. (2001) modelled the near
20 infrared (NIR) region and found that the reflectance around 800 nm is significantly different
21 among species, which differ in intercellular structure. In a common garden experiment,
22 Irisarri et al. (2009) demonstrated that it is possible, using reflectance centred around 820 nm
23 to differentiate between C_3 and C_4 grass compositions.

24 The major challenge, however, is that spectral reflectance data obtained over many narrow
25 contiguous channels (i.e. hyperspectral data) can represent multiple classes that are often

1 mixed for a limited training-sample size (i.e. $n < P$: Chi and Bruzzone 2007). The problem of
2 $n < P$ is associated with the well-described “curse of dimensionality” or the Hughes
3 phenomenon (Hughes, 1968). This phenomenon causes a decrease in a classifier ability to
4 generalize accurately (Ham et al., 2005; Pal and Foody, 2010). Hence, very large training-
5 samples are required to achieve a good description of data distribution (Dalponte et al.,
6 2009). Besides, the Hughes phenomenon often introduces high degree of multicollinearity,
7 caused by the use of highly-correlated predictor variables (Clevers et al., 2007).
8 Multicollinearity is a prominent problem in processing hyperspectral data for vegetation
9 applications, due to similarities in the reflectance properties of biophysical and biochemical
10 characteristics (Ferwerda et al., 2005; Knox et al., 2010; Zhang et al., 2011). The problem of
11 multicollinearity in the matrix of input spectral bands often leads to highly unstable
12 parameter estimates and thus generalization error for a classifier (Bruzzone and Serpico,
13 2000; Clevers et al., 2007).

14 Attempts to solve the problems associated with spectral dimensionality and the related co-
15 linearity include the use of feature reduction and feature selection techniques. The feature
16 selection approach includes those based on a search strategy and on a separability measure.
17 The Sequential Forward Floating Selection (Pudil et al., 1994) and the Steepest Ascent
18 (Serpico and Bruzzone, 2001) are commonly used search strategy techniques, whereas the
19 Bhattacharyya distance (Djouadi et al., 1990), Jeffries–Matusita distance (Bruzzone et al.,
20 1995) and the transformed divergence distance (Su et al., 1990) are examples of the
21 separability measures used in processing hyperspectral data. However, these feature selection
22 techniques require estimation of some statistical properties at full dimensionality, in order to
23 select optimum subset of the input spectral bands for a given classification task. If the
24 training samples are insufficient, the parameterization may not be reliably adequate for the
25 feature selection process (Chi and Bruzzone, 2007).

1 The studies by Schmidt & Skidmore (2003) and Becker et al. (2007) used the approach of
2 analysing the most sensitive wavebands, considering the physical or spectroscopic meaning
3 of each band across the spectrum. This approach often involves the resampling of high-
4 dimensional spectra to wider bandwidths around a few chosen band-centres or to the spectral
5 configuration of existing sensors. In this respect, the sensors respective spectral response
6 functions or spectral resolutions (i.e. Full Width at Half Maximum, FWHM) are simulated.
7 The major limitation of existing resampling methods is that an inherent property of
8 vegetation spectral response is not considered. That is, the asymmetrical nature of correlation
9 between a given waveband (λ) and its shorter and longer wavelength neighbours are not fully
10 accounted for. In this regard, a more innovative approach can be followed, whereby the
11 researchers consider the inter-band correlations around each band centre of interest. The
12 approach has the advantage of linking the physical properties of the target vegetation and its
13 characteristic spectral response function across the spectrum (Schmidt and Skidmore, 2003).
14 When hyperspectral data are processed in this way, classifications are based on the
15 spectroscopic interpretability of each set band (Becker et al., 2007; Faurtyot and Baret, 1997).

16 From this background, the present study sought to classify C₃ and C₄ grass canopies using
17 resampled hyperspectral data obtained through an approach that convolves the spectral
18 information around a chosen given band-centre. The resultant datasets were analysed using
19 the random forest (Breiman, 2001) algorithm. Random forests are advanced non-parametric
20 classifiers, which are increasingly becoming recognized in remote sensing applications
21 involving classification of vegetation (Chan and Paelinckx, 2008; Ghimire et al., 2010; Ismail
22 and Mutanga, 2010; Lawrence et al., 2006). Included in the random forest computation are
23 embedded methods of assessing the generalization error and variable importance measures
24 and the computation does not require tuning of many parameters (Breiman and Cutler, 2004).

25

1 **2. Data acquisition and methods**

2 *2.1. Field spectral data measurements*

3 Field data collection was conducted in the Cathedral Peak region of the Drakensberg
4 Mountain Range, South Africa. The region consists of vegetation divided into altitudinal
5 zones, which correspond closely with the physiographic features of the Drakensberg
6 Mountains (Hill, 1996; Killick, 1963). Three zones namely, the Montane belt (1280 – 1829
7 m), the Sub-alpine belt (1930 – 2865 m) and the Alpine belt (2866 – 3353 m) are defined.
8 These zones also coincide with three terraces in the Drakensberg. These include the river
9 valley system, the foothills (also known as the Little Berg), and the summit areas,
10 respectively. The sub-alpine belt, which is composed of C₃ and C₄ grass species, is also
11 known as the *Themeda-Festuca* sub-alpine grassland (Hill, 1996). This zone is further
12 divided into three grass communities denoted as the *Themeda triandra*, *Festuca costata* and
13 the ‘Mixed’ grasslands. The so-called mixed community consists mainly of variable
14 proportions of C₄ grasses, although the occurrence of *Rendlia altera* seems prevalent.
15 Nonetheless, within the sub-alpine zone there are consociations of the *T. triandra* and the *F.*
16 *costata* species occurrence on warm, northerly and cool, southerly slopes, respectively.

17 Reflectance measurements were collected during the December 2010 summer growing
18 season, using a 2150 band (350–2500 nm resolution) Analytical Spectral Device (ASD), field
19 spectroradiometer (FieldSpec®3 ASD, Inc., Boulder, CO, USA). This device uses a fibre
20 optic cable set at 25° field of view (FOV) to record reflected canopy radiation, which was
21 individually calibrated against a barium sulfate (BaSO₄) white reference panel. Canopy
22 reflectance measurements were collected to characterize the spectral separability among 1×1
23 m sample plots, represented by *F. costata* (C₃), *R. altera* (C₄) and *T. triandra* (C₄) dominant
24 grass species. Spectral reflectance for these dominant grasses (i.e. in the 1×1 m plots) was

1 measured at full canopy cover. Although the dominant grasses co-exist with other species,
2 their respective canopy cover was consistently estimated at $\geq 80\%$ in each target 1×1 m plot.

3 The field spectral measurements were consistently recorded, considering the
4 recommendations in Thenkabail et al. (2000). The ASD optic sensor was held at about 1.5 m
5 directly above the sampling plots, generating an instantaneous field of view of about 0.35 m^2 .
6 A minimum of three positions were randomly chosen within each 1×1 m plot and five
7 spectral measurements were consistently acquired for each one of these positions. This
8 process resulted in a minimum of 15 reflectance measurements per plot. There were no major
9 issues with background effects, since average spectral (\bar{r}_i) measurements for each plot ($i \geq$
10 15) were taken at full canopy cover. A total of 110 plots were measured for each of the three
11 categories of grass species. This process resulted in 330 sample plots, which were considered
12 representative of the spectral variability within and among the grass species under
13 investigation.

14

15 *2.2. Resampling the spectral data*

16 Spectral resampling of the ASD reflectance was conducted using ENVI's spectral
17 resampling routine (ENVI Version 4.7, 2009 Edition, Copyright © ITT Visual Information
18 Solutions). Initially, an ASCII file containing 10-nm-wide band spacing was created and used
19 to aggregate the 1-nm-wide \bar{r}_i spectral data, across the 400-2500 nm spectrum. The ENVI's
20 resampling routine fits a Gaussian model with an FWHM equal to the specified band spacing
21 to resample the data. This initial sampling of the data was carried to aid calculation of the
22 inter-band correlation coefficient matrix of the input spectral bands. The degree of linear
23 relationship between a band and its shorter and longer wavelength neighbours was calculated,
24 using the well-known Pearson's r coefficient of correlation. The linear spectral dependence
25 between two sample wavebands (X_i, Y_i) was assessed, resulting in values between 0 and 1:

$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{X_i - \bar{X}}{s_X} \right) \left(\frac{Y_i - \bar{Y}}{s_Y} \right) \quad (\text{Eq. 1})$$

where $\frac{X_i - \bar{X}}{s_X}$, \bar{X} , and s_X are the standard score, sample mean, and sample standard deviation, respectively (Eq. 1). The Pearson's r correlation coefficient was used, since in this experiment the data assume multimodal normal distribution of the response variables (Chi et al., 2008). The inter-band r coefficient matrix was computed using the R statistical software (R Development Core Team, 2010). The R routines output a spreadsheet file format and an x : y axis contour plot of the inter-band r values.

Spectral response curves were simulated for the predefined thirteen (13) band-centres. The band-centres were chosen on the basis of their known sensitivity to the biophysical and biochemical characteristics of vegetation. Table 1 shows the causal reflectance or absorption features associated with the chosen bands-centres. In addition, the wavelengths (i.e. band-centres) were selected, considering the observed pattern in the matrix of the data points, as depicted in Fig. 1a. Moreover, the chosen band-centres have been reported in the literature to be useful for C₃ and C₄ grass species discrimination. For example, Smith and Blackshaw, (2003) reported high frequencies (>15 out of 20 times) for the band-centres chosen within the visible and near infrared regions. Irisarri et al. (2009) found that the spectral channels around 820 nm were important for differentiating C₃ and C₄ grass compositions. Further, Noble et al. (2002) noted that the chosen bands-centres in the shortwave region are useful for C₃ and C₄ crop/weed species discrimination.

The inter-band Pearson's r correlation coefficient between each of the chosen band-centres and their shorter and longer waveband neighbours was calculated. The band-centres were located at the meeting point of the x: y axis (Fig. 1a), where $r = 1$, and bandwidths were estimated by considering the vertical or the horizontal distance across a given band-centre, as a function of wavelength. It is important to note that the inter-band correlation, r values are

1 asymmetrical across the horizontal or the vertical lines. They are only symmetrical across the
2 diagonal. Therefore, it was possible to capture the spectral response information around each
3 band-centre, using a chosen weighting threshold of inter-band correlation. Various weighting
4 thresholds of user-defined inter-band correlation (WTC $r = 0.99$, WTC $r = 0.95$ and WTC $r =$
5 0.90) were assessed. Fig. 1b illustrates the sizes of the respective user-defined inter-band
6 correlations, using the 660 nm band-centre as an example. The shorter and longer wavelength
7 sides of the sample band-centre (i.e. 660 nm) were calculated on the basis of $r \geq 0.99$, $r \geq$
8 0.95 and $r \geq 0.90$, whereby bands with coefficients beyond a specified WTC were assigned r
9 $= 0$. The procedure was simulated for all the chosen 13 band-centres.

10 The resultant user-defined inter-band correlation filter functions were used in the ENVI's
11 spectral resampling routine. The ENVI's routine assumes a critical spectral resampling when
12 FWHM values are not provided by fitting a Gaussian model with a FWHM equivalent to
13 specified band spacing. However, if a user-defined filter function is incorporated, the routine
14 uses it to simulate each line of wavelengths as a multiplicative factor (i.e. weighting between
15 0 and 1) to resample the data (RSI, 2009). The size of the inter-band correlation for each
16 band-centre varies depending of the chosen WTC and this accounted for the spectral
17 dependence information in the original reflectance data.

18 In addition, conventional approach of resampling reflectance data to match the response of
19 an existing instrument was assessed for comparative purposes, with the proposed user-
20 defined inter-band correlation filter technique. This involves resampling the ASD data to
21 match the Hyperion sensor's (on-board the Earth Observing-1 Satellite) spectral resolution or
22 FWHM function. The procedure is analogous to that of the user-define spectral resampling
23 described. However, the ENVI routine uses the pre-defined spectral library developed for the
24 Hyperion sensor to resample the data. Since the canopy reflectance measurements were
25 conducted under field conditions, the strong noisy incident radiation in 1350-1460 nm, 1790 -

1 1960 nm and inconsistent spectra below 400 nm were removed from all analysis (Thenkabail
2 et al., 2004).

3 4 2.3. *The Random forest's variable importance, classification and accuracy assessment*

5 All the datasets were randomly split into 70% training and 30% holdout test sets ($n = 77$
6 and $n = 33$ subsets, respectively), using the R statistical routine. The random forest algorithm
7 was constructed to grow a large ensemble of classification trees. The resultant trees in the
8 ensemble were used to assign each input spectral bands to a class membership of the response
9 variables: *F. costata*, *R. altera* or *T. triandra*. Each tree is grown from a randomly and
10 independently selected bootstrap sample of the training data, and about one-third, excluded
11 samples, called the out of bag (OOB) samples were used to calculate an unbiased assessment
12 of the classification accuracy (i.e. the OOB error). Since the OOB error is an unbiased
13 assessment of the classification accuracy (Breiman, 2001; Prasad et al., 2006), it provides
14 theoretical guarantee for the groups of C_3 and C_4 grass species detection and classification.
15 Further to using the OOB error samples to assess the overall classification accuracy, the
16 kappa coefficient analysis was performed. This was necessary, since the study involves a
17 multiclass application and the goal is to account for actual agreement specified by each class
18 versus the chance agreement. That is, it was important to determine if one OOB error matrix
19 is significantly different from another (Stehman, 1997).

20 The random forest algorithm is easy to implement, because the user tunes only two
21 parameters: (i) the number of trees (*n_{tree}*) to grow and (ii) the number of variables to split at
22 each node (*m_{try}*). The default value of the *m_{try}* parameter in the context of classification
23 applications is denoted by the square root of the total number of input variables (Liaw and
24 Wiener, 2002). In the current analysis, the OOB error samples for each class membership of

1 the input spectral bands were used to optimize the *n*tree and *m*try hyper-parameters (Ismail
2 and Mutanga, 2011).

3 The random forest-based variable permutation mean decrease in accuracy (Strobl and
4 Zeileis, 2008) was used to calculate the importance of each predictor variable. The variable
5 rankings were calculated using all variables (i.e. 70% training set) and optimize *m*try value
6 based on the specified *n*tree (i.e.10 000 for all datasets) value. To decrease computing time
7 the routine starts with the default *m*try value for each dataset and then calculates to the right
8 of the value; and then to the left of the value. For example, the default *m*try for the resampled
9 Hyperion dataset (n = 197) is 14, so the routine uses *m*try values of 2, 7... to the left (deflate)
10 of the default value; and *m*try values of 28, 42... to the right (inflate) of the default *m*try
11 value. It then runs the random forest based on the optimized *m*try and *n*tree values and
12 determines variable rankings and the test dataset error.

13

14 *2.3.1. Random forest-based fast forward variable selection*

15 To calculate the greedy fast forward variable selection (FvS) using the OOB error rates
16 (Adam et al., 2009; Dye et al., 2011), the routine uses the optimized random forest variable
17 rankings calculated above to create different subsets of variables. It involves iteratively fitting
18 the random forest model on the 70% training datasets, and at each iteration building a new
19 model by adding the band with highest importance. Consequently, the routine optimizes the
20 *m*try and *n*tree values for each step of the variable selection process. To decrease computing
21 time the routine was set to terminate at the iteration with subset OOB error less than the
22 overall OOB error calculated when using all the variables. This can be calculated to include a
23 percentage improvement of the overall OOB error. However, because the input Hyperion
24 bands (n = 197) are high in dimension (more than 100 predictors variables), the percent
25 improvement approach was not exploited for the current application.

1 Several empirical evidences have shown that the random forest algorithm shows
2 significant preference towards highly correlated predictor variables (Nicodemus et al., 2010;
3 Strobl et al., 2008). The authors reported that traditional random forest's preference for
4 highly-correlated predictor variables can be carried forward to any significance test or
5 variable selection processes constructed from the importance measures. In this respect,
6 researchers have suggested the use of conditional variable importance approach to mitigate
7 the problems associated with traditional random forest variable selection process. Despite the
8 recommendation, in the current experiment assesses the random forest-based FvS process on
9 the highly dimensional resampled Hyperion bands, for comparative purposes with the WTC
10 datasets.

11

12 **3. Results**

13 *3.1. The user-defined inter-band correlation filter technique of spectral resampling*

14 The results obtained indicate that large portions of the C₃ and C₄ grass canopy reflectance
15 exist in highly correlated wavelengths. In general, a decrease in spectral resolutions was
16 observed for each of the 13 band-centres in relation to the user-defined weighting thresholds
17 of inter-band correlation filter: $r = 0.99$, $r = 0.95$ and $r = 0.90$, respectively. For each derived
18 waveband, the inter-band correlation coefficient $r = 1$ at the band-centres and generally
19 decreases across the shorter or longer wavelengths neighbours, as quantified by a chosen
20 WTC filter. Overall, the WTC $r = 0.99$ filter yielded higher spectral resolutions, among the
21 three filters assessed. In addition, it appeared that the band-centres of specific regions (i.e. the
22 visible, red-edge, near infrared and shortwave infrared spectra) showed varying degrees of
23 inter-band correlations, resulting in variable spectral resolutions, for each of the spectral
24 regions. Table 2 shows the results of the various spectral resolutions obtained for each band-
25 centre of the WTC datasets.

3.2. C_3 and C_4 grass species classification using the WTC and resample Hyperion datasets

The random forest hyper-parameters were optimized using the OOB error rates. The WTC, $r = 0.99$ filter yielded the highest classification accuracy among the three user-defined thresholds of inter-band correlation filters assessed. Table 3 shows the overall accuracies (OOB error rates) and the kappa coefficients obtained for all datasets, including the resampled Hyperion. The OOB error and kappa coefficients increased substantially when the WTC of $r = 0.90$ filter dataset was analyzed. However, the results obtained showed that the proposed user-defined thresholds of inter-band correlation filter approach to resampling Hyperspectral data produced higher classification accuracies when compared with the conventional technique of resampling data to match the Hyperion sensors spectral resolution.

Although the WTC datasets yielded significantly variable classification accuracies, a similar variable importance ranking was obtained for these datasets. Consequently, only the variable importance ranks of the WTC $r = 0.99$ dataset is presented in Fig. 2. Since the random forest algorithm was initially run using all the resampled Hyperion bands ($n = 197$), the variable importance measure (Fig. 3) was then exploited to evaluate whether the FvS process could improve the classification accuracy. This procedure yielded an optimal subset of 22 bands (Table 4), which were subsequently used to classify the C_3 and C_4 response variables. The results obtained showed that the resampled Hyperion band B7 yielded the highest mean decrease in accuracy (11.13%), and that was subsequently carried over to the variable (1/197 bands) selection process. It should be noted that only the optimum subset of the best ranked bands are reported in Table 4. Inter-band correlation coefficient matrix (Table 5) of the optimal subset of bands selection through the random forest-based FvS process was exploited. As expected, the results showed clearly that the FvS procedure yielded highly correlated resampled Hyperion bands and that the majority of the selected bands were concentrated in specific regions of the spectrum.

1

2 **4. Discussion**

3 Hyperspectral data are suitable for C₃ and C₄ grass species classification, since spectral
4 fine features characteristic of vegetation is more discernible from narrowband sensors.
5 However, it can be challenging to classify C₃ and C₄ grass species using their spectral
6 reflectance data, due to the problem of hyper-dimensionality and associated multicollinearity
7 phenomena (Pal and Foody, 2010). Among other factors (e.g. Phenological effects and solar
8 illumination conditions), spectral similarity between C₃ and C₄ grasses and their co-existing
9 species can have significant impacts on the classification capability of canopy reflectance
10 data (Schmidt and Skidmore, 2001). Despite these challenges, recent studies have shown that
11 subtle differences in structural and physiological properties, such as those described for C₃
12 and C₄ grasses may be detected by leaf or canopy reflectance (Irisarri et al., 2009; Liu and
13 Cheng, 2011).

14 Although previous studies have used narrow-band spectral data to classify grasslands of C₃
15 and C₄ species composition, the present investigation explores the potential use of a user-
16 defined inter-band correlation filter to resample hyperspectral data, for subsequent
17 classification analysis. This study demonstrated the trade-offs between retaining narrow
18 bands spectral data vs. the optimal reduction in spectral dimensionality for improved
19 classification. The results obtained explained the spectroscopic interpretability of the chosen
20 band-centres, in reference to their sensitivity to leaf or canopy surface properties, internal
21 structure and biochemical concentrations. These characteristic features are known to
22 significantly vary between C₃ and C₄ grass species. Hence, variations in pigments content,
23 nitrogen, carbon compounds (lignin and fibre) and water components (inter-cellular air-
24 moisture or leaf liquid water content) can be attributed to the good spectral separability
25 obtained for the target grasses assessed in this study. In general, the results have shown that

1 the proposed user-defined inter-band correlation filter technique yielded improved
2 classification of *F. costata*, *R. altera* and *T. triandra* grass canopies. More detailed analyses
3 of the results are presented next: the weighting thresholds of inter-band correlation filter
4 approach to resampling hyperspectral data; the random forest classification and band subset
5 selection of resampled Hyperion dataset, using a traditional method vs. prior dimensionality-
6 reduction, using the WTC filter technique and; implications of the present investigation for
7 applications involving C₃ and C₄ grass species.

8

9 *4.1. The weighting thresholds of inter-band correlation filter approach*

10 On the basis of the proposed resampling approach, this study has shown that highly
11 correlated hyperspectral wavebands in specific regions can be optimally aggregated to reduce
12 spectral dimension of the input spectral bands. The proposed spectral resampling technique
13 takes advantage of the inherent property of vegetation reflectance, the asymmetrical nature of
14 the inter-band correlation matrix of the collected wavebands. The results presented in Table
15 2 show the extent of spectral convolution using the highly correlated wavelengths around
16 each of the selected band-centres across the 400 – 2500 nm spectrum. The vegetation spectral
17 response property used to calculate the various WTC *r* values (i.e. 0.99, 0.95 and 0.90) can be
18 attributed to reflectance or absorption features characteristic of the target C₃ and C₄ grasses
19 (Ferwerda et al., 2005; Knox et al., 2010). In a previous study, Slanton et al. (2001) found
20 800 nm wavelength contained very strong discriminating power for plant species at the level
21 of leaf internal structure. Further, Irisarri et al. (2009) reported that vegetation reflectance at
22 the 820 nm spectral range is sensitive to even subtle differences among grass species or
23 between groups of C₃ and C₄ grasses. Hence, in the present experiment, the user-defined inter-
24 band WTC filters were used to assess the optimal spectral resolutions around chosen band-
25 centres, including the 820 nm wavelength. In this regard, the proposed resampling procedure

1 offers the potential for data dimensionality reduction and optimizes elimination of redundant
2 spectral information by means of weighting thresholds of inter-band correlation criterion.

3 It is worth noting that the newly introduced resampling approach not only reduces
4 dimensionality in hyperspectral data, it also preserves relevant spectral information for
5 posterior classification of C₃ and C₄ grass canopy reflectance. In general, there is very close
6 relationship between classifier sensitivity to data dimensionality and classification accuracy,
7 under conditions of multiple correlations among the input spectral bands (Gomez-Chova et
8 al., 2003). This suggests the concept of using spectral resampling techniques capable of
9 reducing co-linearity problems in the input spectral space, for applications involving C₃ and
10 C₄ grass species.

12 *4.2. Random forest-based band subset selection vs. prior dimensionality-reduction*

13 Random forests have been found attractive for the analysis of remotely sensed data for
14 ecological applications (Chan and Paelinckx, 2008; Ham et al., 2005; Lawrence et al., 2006;
15 Prasad et al., 2006). A number of studies have asserted that the method is insensitive to high-
16 dimensionality and, therefore, does not require a dimensionality-reduction analysis in pre-
17 processing (Breiman and Cutler, 2004; Ham et al., 2005). However, the assessment of
18 random forest's variable importance measure in high-dimensional spectral space, has
19 revealed that the algorithm thus show a preference to highly correlated predictor variable.
20 Such a preference was also found to be manifest in the subsequent subset band selection
21 process (Table 5). The results from the present experiment thus reaffirm the findings of the
22 recent studies, which investigated random forests variable importance under predictor
23 correlation and the generalization of parameter estimates (Nicodemus and Shugart, 2007;
24 Strobl et al., 2008). In their studies, the authors recommended conditional variable
25 importance approach for random forest-based variable selection and posterior classifications.

1 Critically, the results obtained from the present study showed that WTC $r = 0.99$ yielded
2 the highest classification accuracy ($\kappa = 0.82$) among the three inter-band correlation
3 thresholds assessed. This superior accuracy demonstrates clearly, the role of spectral
4 resolutions on C_3 and C_4 grass classification and the classifier accuracy. However, the larger
5 decrease in classification accuracy obtained for WTC $r = 0.90$ could be attributed to the very
6 larger increase in wavelengths for each individual waveband, as represented in Table 2. The
7 trend obtained among the classification of the three WTC r datasets compares well with
8 Dalponte et al. (2009), who investigated the effect of changing spectral resolution upon
9 different classifiers for forest applications. In their study, the authors found that as spectral
10 resolutions were degraded from 4.6 nm to 36.8 nm, overall κ accuracies dropped from ~
11 89 % to ~ 84 %, respectively, using Support vector machines (SVM) algorithm (Vapnik,
12 1998). Furthermore, when compared with classification involving a simple parametric
13 classifier such as LDA, Dalponte et al. (2009) recorded inferior κ accuracies which also
14 dropped from ~ 77 % to ~54 %, respectively. The authors concluded that advanced non-
15 parametric classifiers, such as the random forest are more applicable for classifications
16 involving complex vegetation feature spaces.

17 As depicted on Table 5, the random forest band selection process showed a significant bias
18 toward the highly correlated Hyperion bands (e.g. B6 - B13 and B198 - B219). However, the
19 random forest analysis on the prior dimensionality-reduction datasets offered distinct
20 advantage, using the inter-band correlation WTC filters to aggregate the majority of the
21 highly correlated wavebands. The novelty of the proposed method is that the bands
22 contributing to the out reflectance data were weighted according to their linear relationship
23 with a chosen band-centre. The resultant classification accuracies showed that the prior
24 dimensionality-reduction approach considerably negates problems associated with spectral
25 redundancy and thereby mitigated against the multicollinearity phenomenon (Gomez-Chova

1 et al., 2003). Furthermore, the present experiment has demonstrated that even when a large
2 training sample (i.e. 330 canopy spectra), compared to the number of spectral bands ($n = 197$)
3 are used, spectral filtering may still be useful. This affirmation is supported by the accuracy
4 derived from the use of the optimized 13 bands, which yielded superior classification
5 accuracies (OOB = 0.14; kappa 0.82), compared to that derived from the use of a larger but
6 high-correlated resampled Hyperion bands (OOB = 0.19; kappa = 0.76).

7

8 *4.3. Implications of the present investigation and conclusion*

9 The primary purpose of this study was to assess the spectral separability among C_3 and C_4
10 grasses, sampled from the Drakensberg Mountains of South Africa. The secondary goal was
11 to address the issue of multicollinearity effect on the performance of the random forest
12 variable importance and the subsequent band subset selection process under predictor
13 correlation. The performance of the method, when applied to data derived by resampling
14 spectra to the Hyperion sensor's spectral resolution, was compared to that of spectra
15 resampled by weighting the inter-band correlations, as a function of wavelength. The overall
16 implications for this investigation are related to various hyperspectral data application
17 constraints: i) the trade-off between the number of spectral bands and the resolution of
18 remotely sensed imagery; ii) the trade-off between higher spectral resolution and reduced
19 signal-to-noise ratio, and iii) challenges associated with the optimal configuration of
20 wavebands capable of providing sensitive information about a target vegetation (Price, 1994;
21 Thenkabail et al., 2004). Therefore, in the present experiment, a technique has been proposed
22 to reduce dimensionality, while preserving relevant spectral information for posterior
23 classification task. It has been observed that the proposed resampling technique represents a
24 potential method of reprogramming hyperspectral resolutions and band configurations. This
25 potential also holds prospects in the development and configuration of future remote sensors

1 to collect optimal spectral resolutions and configuration for specific vegetation applications.
2 The results obtained in this study suggested that further studies addressing multicollinearity
3 problem should consider techniques that account for the spectral dependence information
4 contained in vegetation reflectance data. In summary, the current technique described in this
5 paper yields the following distinct benefits:

- 6 • Reduces data dimensionality by accounting for the inter-band correlations around
7 specific band-centres of interest and thereby mitigating against the multicollinearity
8 phenomenon caused by highly correlated spectral bands.
- 9 • Optimizes the spectral resolutions useful for the separability among the dominant C₃
10 and C₄ grass species investigated.
- 11 • Assists the random forest, to achieve improved classification accuracy, thereby
12 providing the potential to link each individual input band to the physical meaning of
13 interaction effects in the structure of the acquired data.

14

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18 Wildlife.

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23

1 Figure captions

2 Fig. 1 Pearson's r correlation coefficients matrix (plot) of the input spectral bands, calculated
3 using reflectance data aggregated into 10-nm-wide band intervals (a) and an
4 illustration of the user-defined inter-band correlation filter for 660 nm band-centre (b).

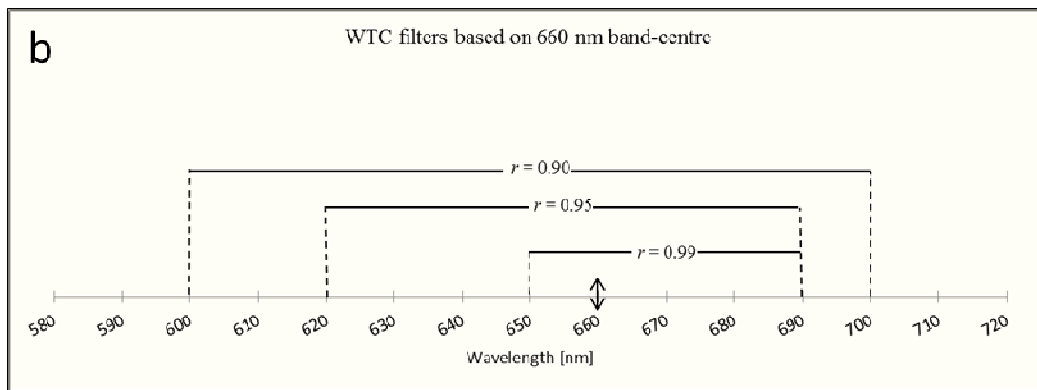
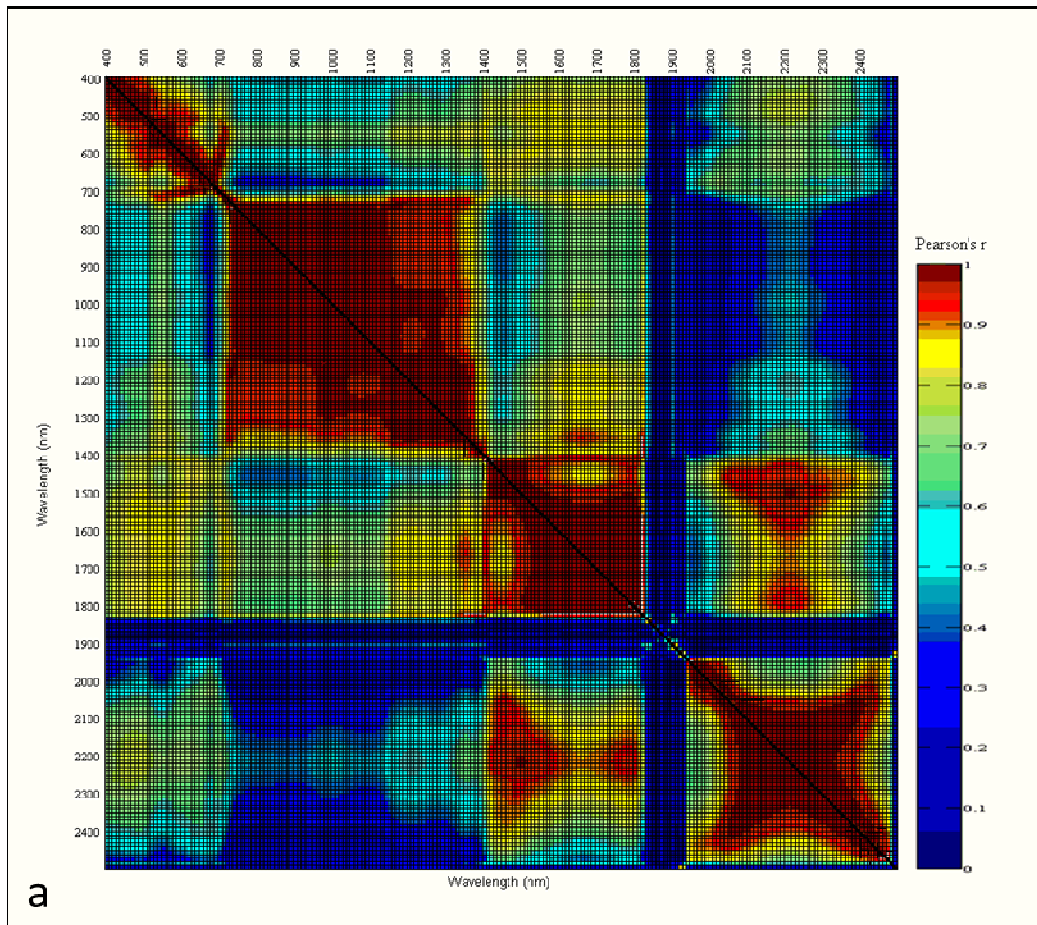
5

6 Fig. 2 Random forests variable importance ranks for the WTC $r = 0.99$ dataset ($n = 13$ bands)
7 based on the Mean Decrease in Accuracy values. The reflectance spectrum of the
8 target grass species is shown.

9

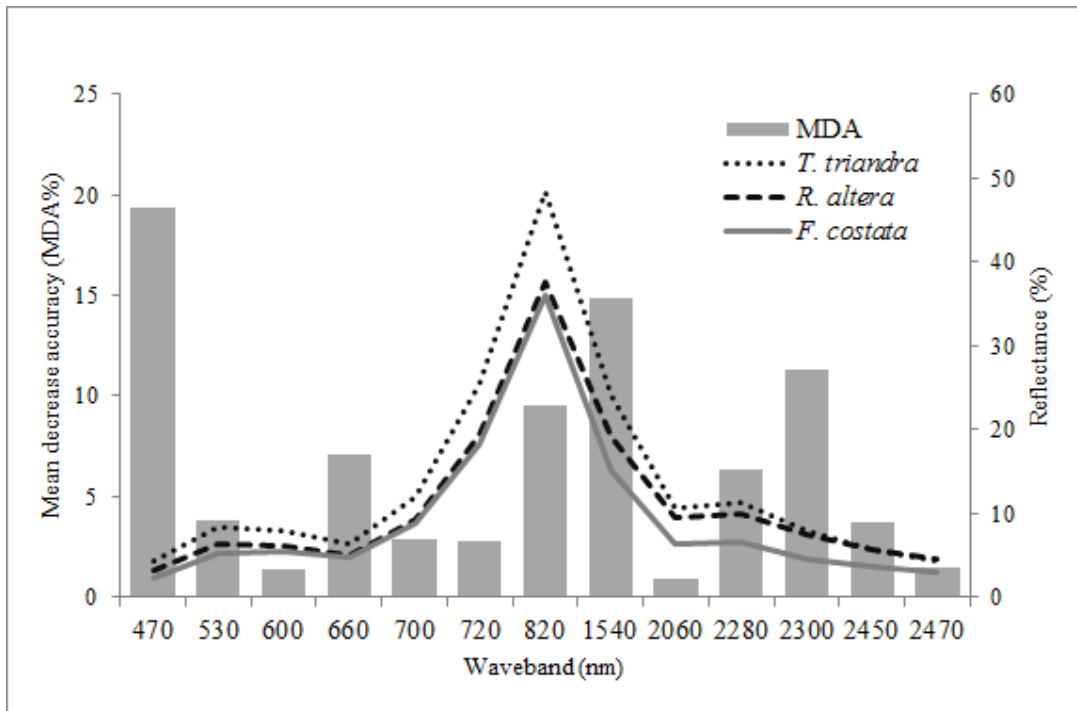
10 Fig. 3 Random forests variable importance ranks for resampled Hyperion bands ($n = 197$)
11 based on the Mean Decrease in Accuracy values. The reflectance spectrum of the
12 target grass species is shown.

13



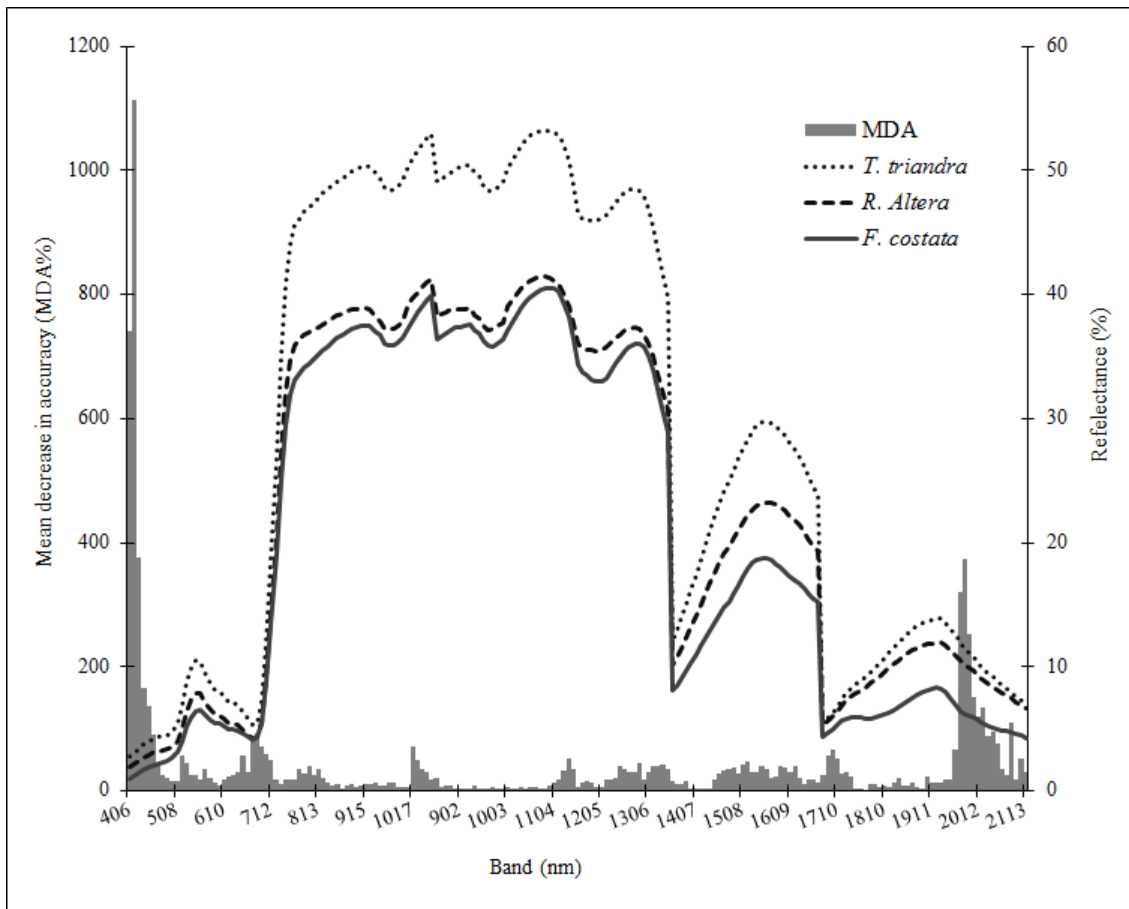
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Table 1

Wavelengths corresponding to known absorption features, as described in previous studies to be highly sensitive to the properties of reflection or absorption of vegetation structural and biochemical characteristics.

No.	Band (nm)	Known Causal compound/ feature	Source
1	470	Total plant pigment concentration	Blackburn, 1998
2	530	Chlorophyll a absorption	Gamon et al., 1997
3	600	Nitrogen	Faurtyot and Baret, 1997
4	660	Nitrogen	Curran, 1989
5	700	Total Chlorophyll, Nitrogen	Carter, 1994
6	720	Total Chlorophyll, Leaf mass	Horler et al., 1983
7	820	Leaf mass, Leaf area index	Curran, 1989
8	1540	Cellulose, vegetation water content	Carter, 1994
9	2060	Protein	Carter, 1994
10	2280	Cellulose, Sugar, Starch, Leaf mass	Curran, 1989
11	2300	Leaf mass, vegetation water content	Carter, 1994
12	2450	Cellulose, Protein, Nitrogen	Carter, 1994
13	2470	Cellulose, Protein	Kumar et al., 2001

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Table 2

Spectral resolutions obtained from the analysis of the user-defined inter-band correlation.

Band centre (nm)	Wavelength (nm) filter size/ Resampled datasets		
	WTC $r = 0.99$	WTC $r = 0.95$	WTC $r = 0.90$
470	430 - 500	410 - 520	400 - 530
530	520 - 570	500 - 600	470 - 600
600	580 - 630	550 - 650	530 - 660
660	650 - 690	620 - 690	600 - 700
700	700*	690 - 710	690 - 710
720	720*	710 - 730	710 - 740
820	740 - 1110	730 - 1190	730 - 1330
1540	1500 - 1630	1470 - 1780	1470 - 1780
2060	2040 - 2090	2020 - 2180	1990 - 2280
2280	2100 - 2300	2060 - 2300	2060 - 2300
2300	2300 - 2350	2280 - 2390	2289 - 2420
2450	2450*	2410 - 2460	2360 - 2470
2470	2470*	2460 - 2470	2450 - 2470

* Indicates wavelength = 10 nm of the input spectral band.

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Table 3

Random forest model optimization and accuracy measures using OOB samples on the training dataset (70% sample). The Kappa-test set statistics were calculated using 30 % holdout samples.

Resampled datasets	Number of Bands	Optimized <i>mtry</i>	Optimized <i>ntree</i>	OOB error rate	Kappa Training set	Kappa-Test set
Resampled-Hyperion	197	56	500	0.19	0.71	-
Resampled-Hyperion	22	20	1500	0.19	0.72	0.76
WTC $r = 0.99$	13	6	4000	0.14	0.79	0.82
WTC $r = 0.95$	13	3	2500	0.21	0.68	0.79
WTC $r = 0.90$	13	9	4000	0.23	0.64	0.76

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Table 4

Random forest-based forward best ranked band selection on resampled-Hyperion spectral resolution. The Kappa statistics were calculated on 70 % training sample.

Rank	Hyperion band	Average wavelength (nm)	FWHM (nm)	Optimized <i>mtry</i>	Optimized <i>ntree</i>	Accuracy: cumulative OOB
1	B7	416.64	11.39	1	500	0.518
2	B6	406.46	11.39	2	10000	0.595
3	B212	2274.42	10.43	3	1000	0.693
4	B211	2264.32	10.44	4	1500	0.68
5	B8	426.82	11.39	4	500	0.693
6	B213	2284.52	10.42	4	7500	0.699
7	B9	436.99	11.39	7	1500	0.706
8	B216	2314.81	10.41	1	7000	0.699
9	B214	2294.61	10.41	6	500	0.706
10	B215	2304.71	10.41	6	2500	0.693
11	B217	2324.91	10.41	9	1000	0.693
12	B10	447.17	11.39	12	500	0.706
13	B210	2254.22	10.46	1	500	0.699
14	B12	467.52	11.39	8	500	0.712
15	B218	2335.01	10.41	2	1000	0.725
16	B11	457.34	11.39	4	500	0.725
17	B219	2345.11	10.41	4	6500	0.732
18	B33	681.2	10.33	18	500	0.771
19	B198	2133.24	10.73	8	500	0.771
20	B200	2153.34	10.68	4	1000	0.764
21	B158	1729.7	11.56	20	1000	0.803
22	B13	477.69	11.39	20	1500	0.81

3

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Table 5
High correlated variables from random forest's importance rank and selection process.

	Resampled Hyperion Wavelength (nm)																							
	406.46	416.64	426.82	436.99	447.17	457.34	467.52	477.69	681.2	1729.7	2133.24	2153.34	2254.22	2264.32	2274.42	2284.52	2294.61	2304.71	2314.81	2324.91	2335.01	2345.1		
406.46	1																							
416.64	0.99	1																						
426.82	0.99	0.99	1																					
436.99	0.99	0.99	0.99	1																				
447.17	0.99	0.99	0.99	0.99	1																			
457.34	0.98	0.99	0.99	0.99	0.99	1																		
467.52	0.98	0.98	0.99	0.99	0.99	0.99	1																	
477.69	0.97	0.98	0.99	0.99	0.99	0.99	0.99	1																
681.2	0.74	0.77	0.79	0.81	0.82	0.83	0.85	0.87	1															
1729.7	0.87	0.88	0.89	0.9	0.9	0.9	0.91	0.91	0.78	1														
2133.24	0.85	0.85	0.86	0.86	0.87	0.87	0.87	0.87	0.78	0.93	1													
2153.34	0.85	0.86	0.86	0.87	0.87	0.88	0.88	0.88	0.79	0.94	0.99	1												
2254.22	0.86	0.87	0.87	0.87	0.88	0.88	0.88	0.88	0.77	0.95	0.99	0.99	1											
2264.32	0.86	0.86	0.87	0.87	0.87	0.87	0.87	0.87	0.76	0.94	0.99	0.99	0.99	1										
2274.42	0.86	0.86	0.86	0.87	0.87	0.87	0.87	0.87	0.76	0.93	0.99	0.99	0.99	0.99	1									
2284.52	0.85	0.86	0.86	0.86	0.86	0.87	0.87	0.87	0.76	0.93	0.99	0.99	0.99	0.99	0.99	1								
2294.61	0.85	0.85	0.86	0.86	0.86	0.86	0.86	0.86	0.77	0.93	0.99	0.99	0.99	0.99	0.99	0.99	1							
2304.71	0.84	0.84	0.85	0.85	0.85	0.85	0.85	0.85	0.76	0.92	0.99	0.99	0.99	0.99	0.99	0.99	0.99	1						
2314.81	0.83	0.84	0.84	0.84	0.84	0.85	0.85	0.85	0.76	0.91	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	1					
2324.91	0.83	0.83	0.84	0.84	0.84	0.84	0.84	0.84	0.76	0.9	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	1				
2335.01	0.82	0.82	0.83	0.83	0.83	0.83	0.84	0.84	0.76	0.9	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	1			
2345.11	0.81	0.82	0.82	0.82	0.83	0.83	0.83	0.83	0.76	0.89	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	0.99	1	

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