

# Experimental generation and application of the superposition of higher-order Bessel beams

**A. Dudley<sup>1,2</sup> R. Vasilyeu<sup>3</sup>, A. Forbes<sup>1,2,4</sup>, N. Khilo<sup>3</sup> and P. Ropot<sup>3</sup>**

<sup>1</sup> CSIR National Laser Centre

<sup>2</sup> School of Physics, University of KwaZulu-Natal

<sup>3</sup> B.I. Stepanov Institute of Physics, National Academy of Sciences of Belarus

<sup>4</sup> School of Physics, University of Stellenbosch

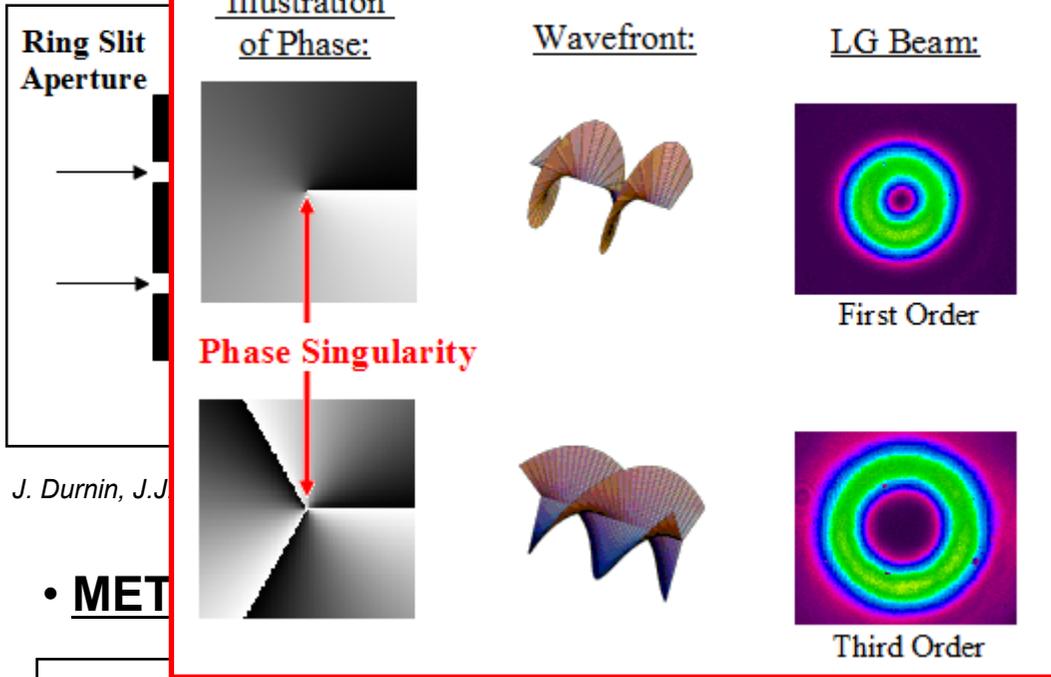
*Presented at the  
2009 South African Institute of Physics Annual Conference  
University of KwaZulu-Natal  
Durban, South Africa  
6-10 July 2009*



# Generation of Bessel Fields:

• MET

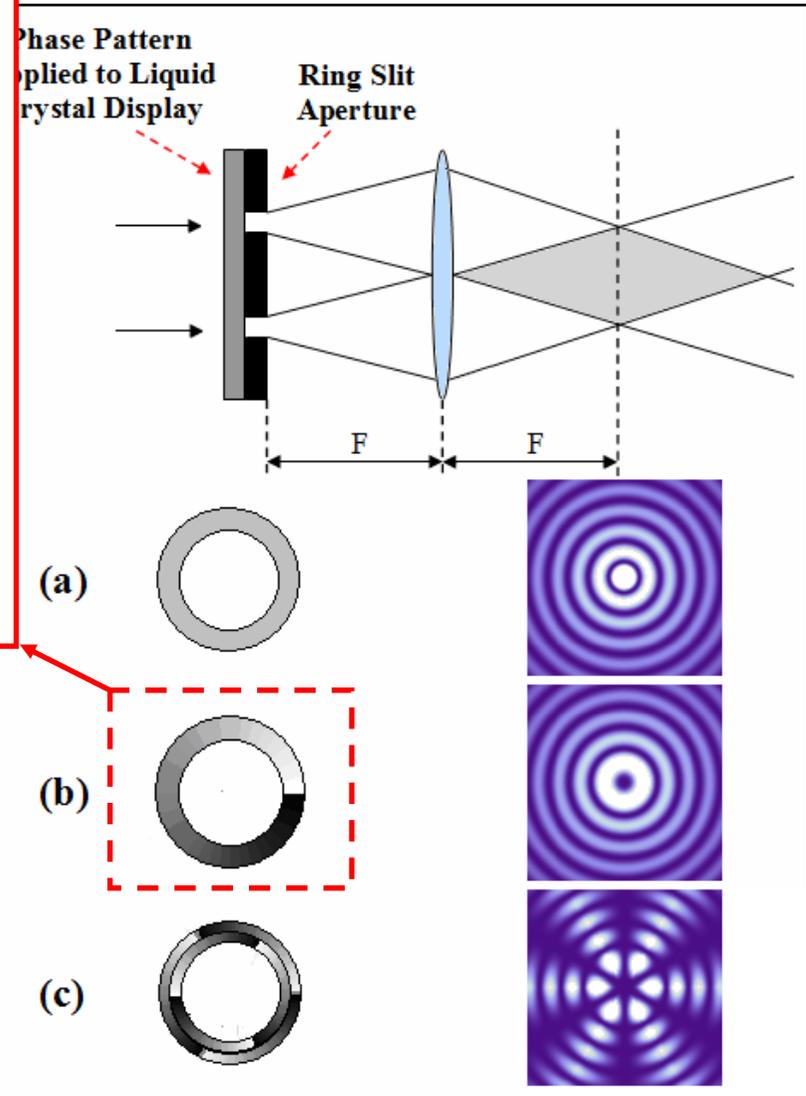
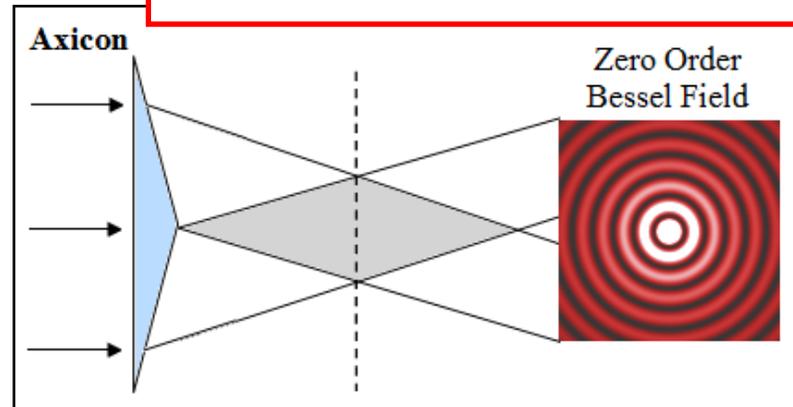
## Azimuthal Phase Dependence:



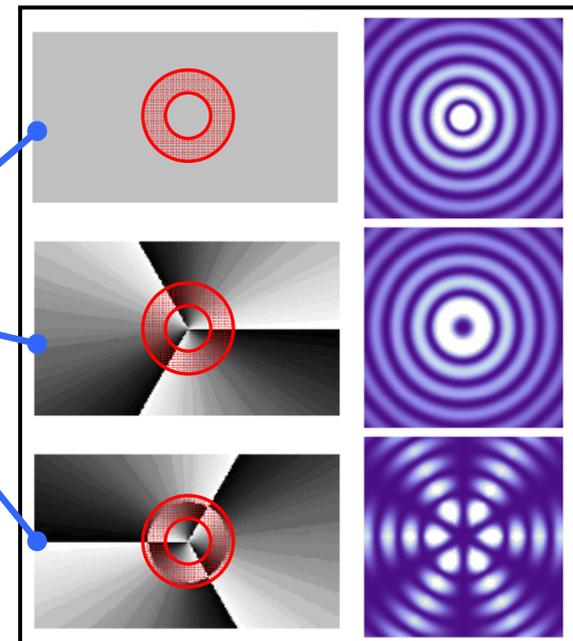
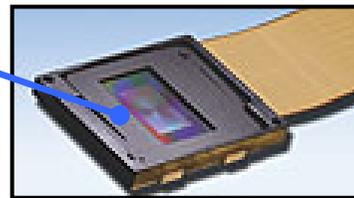
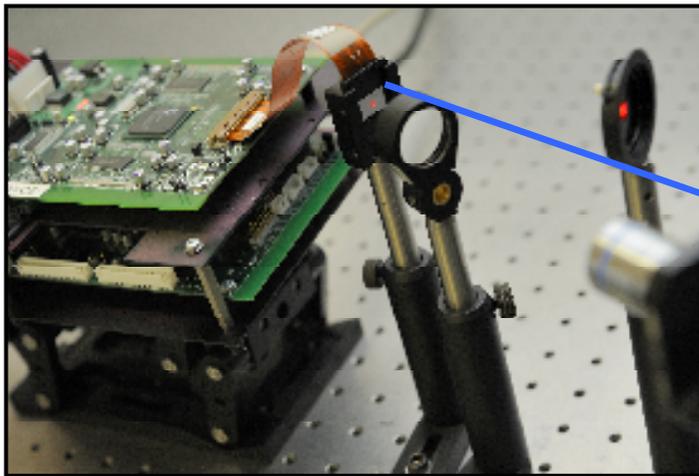
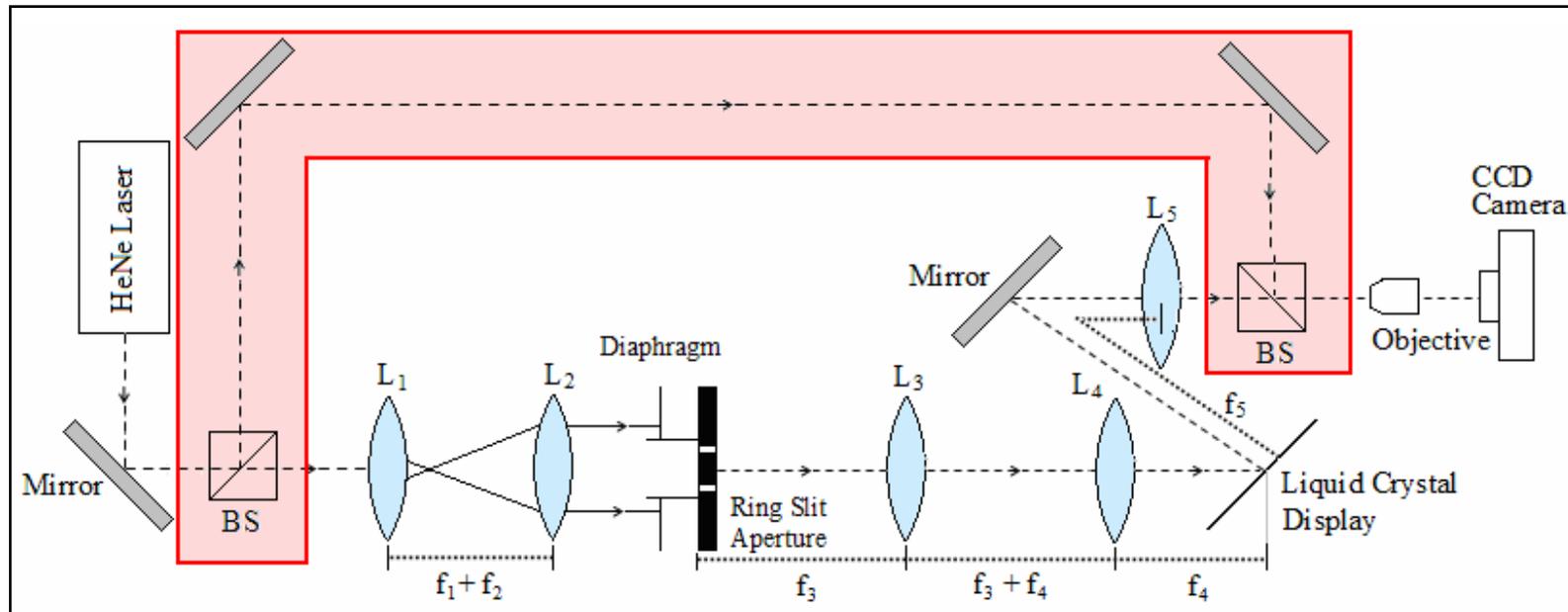
J. Durnin, J.J

• MET

Adaptation of method 1 to produce superpositions of higher-order Bessel beams:



# Experimental Setup:



# Theoretical Background:

Transmission function of ring slit aperture:

$$\tau(r, \varphi) = \begin{cases} \exp(im\varphi) & R \geq r \geq (R - \Delta) \\ \exp(in\varphi) & R \leq r \leq (R + \Delta) \end{cases}$$

Diffraction Integral:

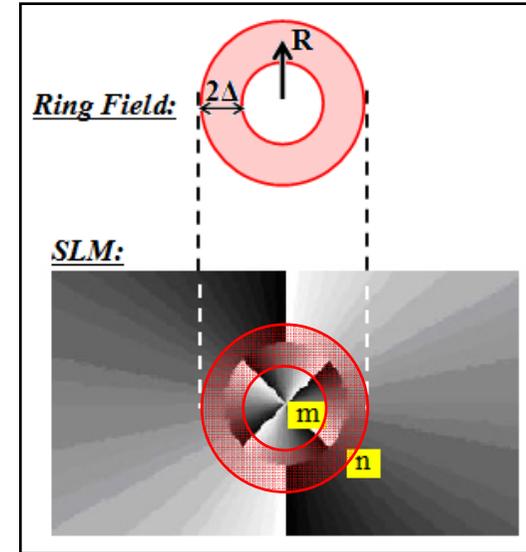
$$A(r, \varphi, z) = \frac{-i}{\lambda z} \int_0^{2\pi} \int_{R-\Delta}^{R+\Delta} \tau(r, \varphi) \exp\left[i \frac{k_0}{2f} \left(1 - \frac{z}{f}\right) r^2\right] \exp\left[-i \frac{k_0 r r_1}{f} \cos(\varphi_1 - \varphi)\right] r_1 dr_1 d\varphi_1$$

Resulting Field:

$$A_{m,n}(r, \varphi, z) = A_m(r, \varphi, z) + A_n(r, \varphi, z)$$

$$A_m(r, \varphi, z) = \frac{-ik_0}{f} \int_{R-\Delta}^R \left( i^m \exp(im\varphi) J_m\left(\frac{k_0 r r_1}{f}\right) \right) \exp\left[-\frac{r_1^2}{w^2} + \frac{ik_0 r_1^2}{2f} \left(1 - \frac{z}{f}\right)\right] r_1 dr_1$$

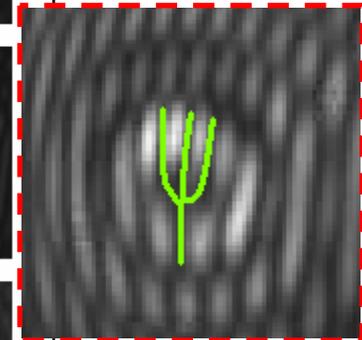
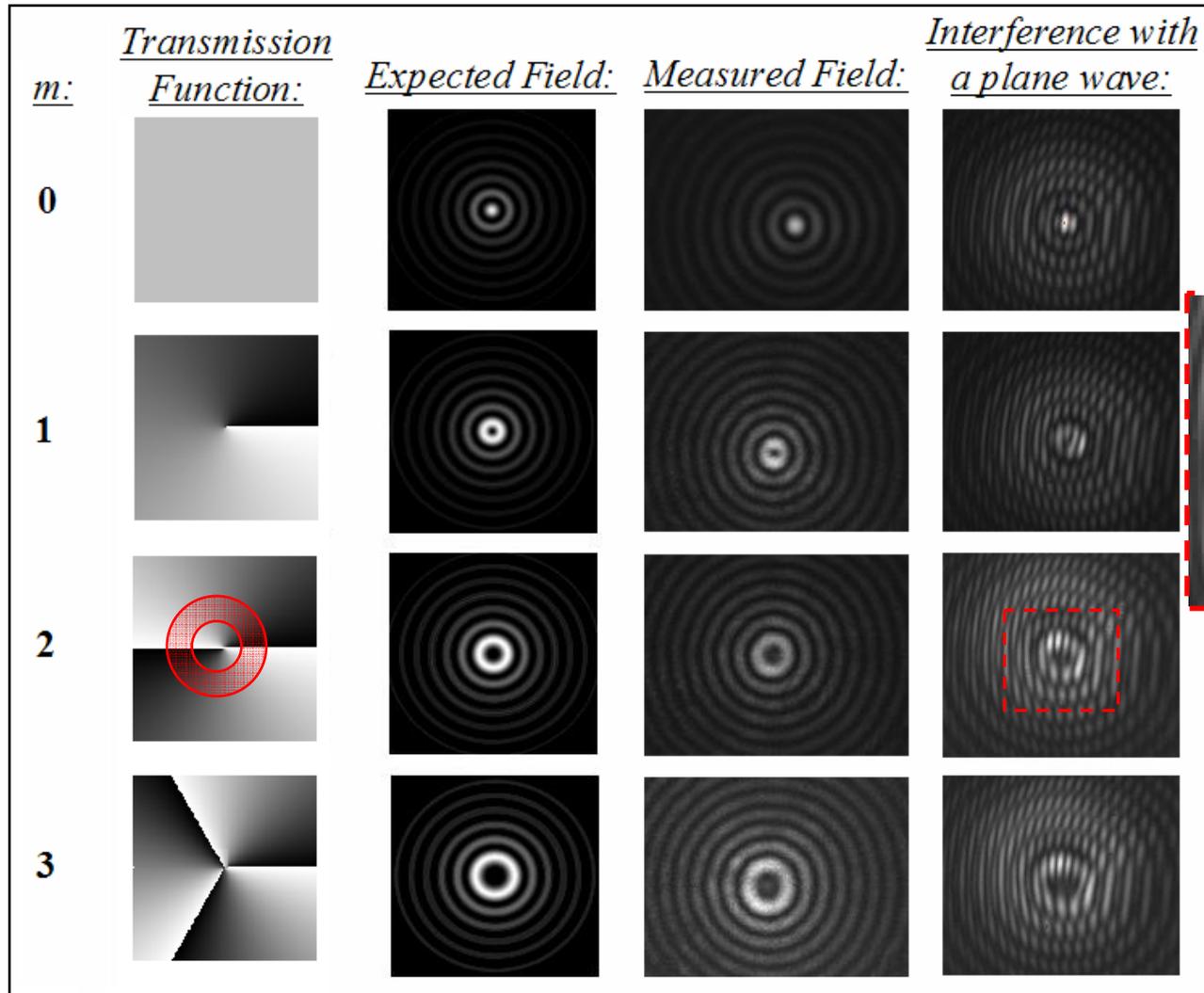
$$A_n(r, \varphi, z) = \frac{-ik_0}{f} \int_R^{R+\Delta} \left( i^n \exp(in\varphi) J_n\left(\frac{k_0 r r_1}{f}\right) \right) \exp\left[-\frac{r_1^2}{w^2} + \frac{ik_0 r_1^2}{2f} \left(1 - \frac{z}{f}\right)\right] r_1 dr_1$$



# Experimental Results: Single Bessel Field

Transmission Function:  $\tau(r, \varphi) = \exp(im\varphi) \quad (R + \Delta) \geq r \geq (R - \Delta)$

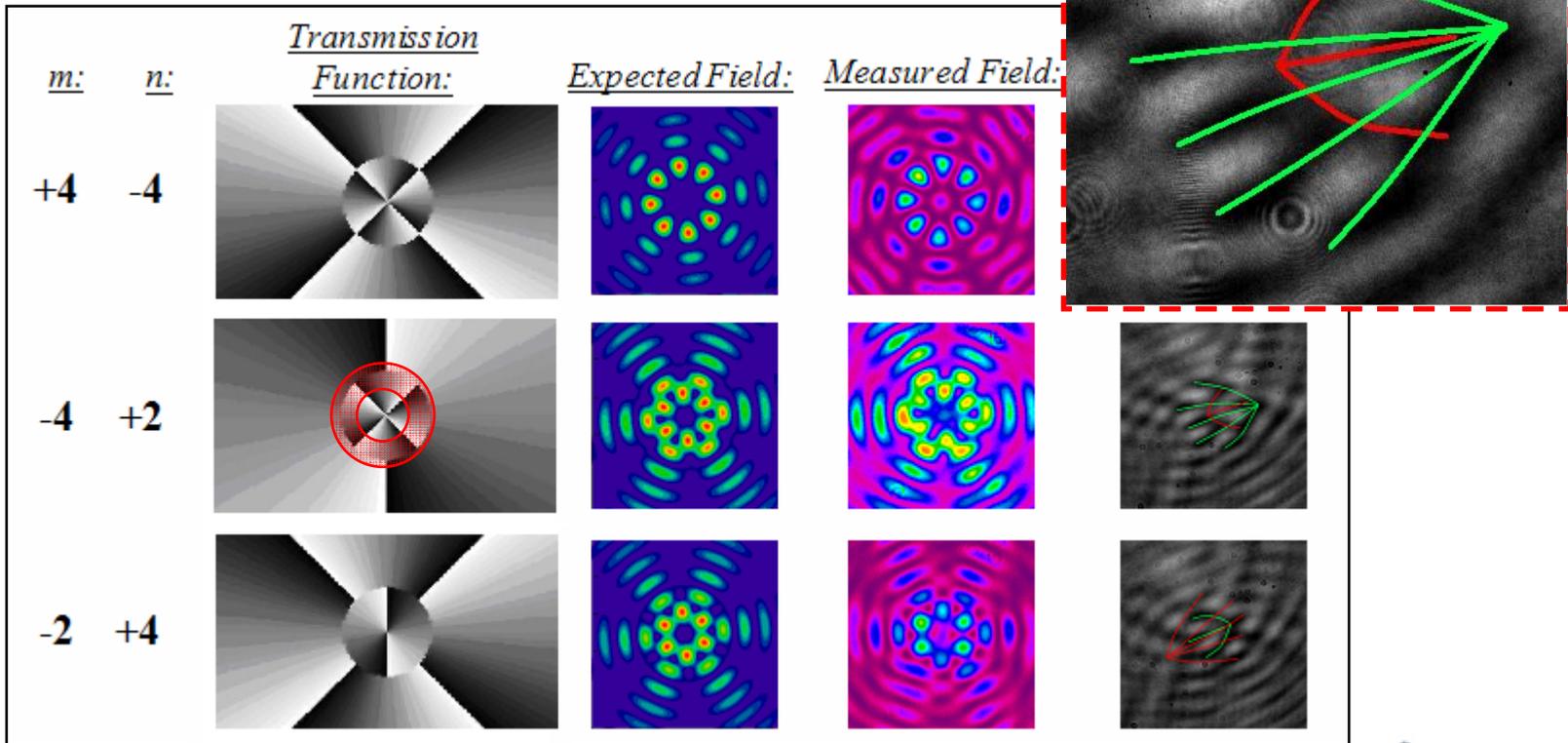
Resulting Field:  $A_m(r, \varphi, z) \propto J_m\left(\frac{k_0 r}{f}\right)$



# Experimental Results: Superposition of 2 Bessel Fields

Transmission Function: 
$$\tau(r, \varphi) = \begin{cases} \exp(im\varphi) & R \geq r \geq (R - \Delta) \\ \exp(in\varphi) & R \leq r \leq (R + \Delta) \end{cases}$$

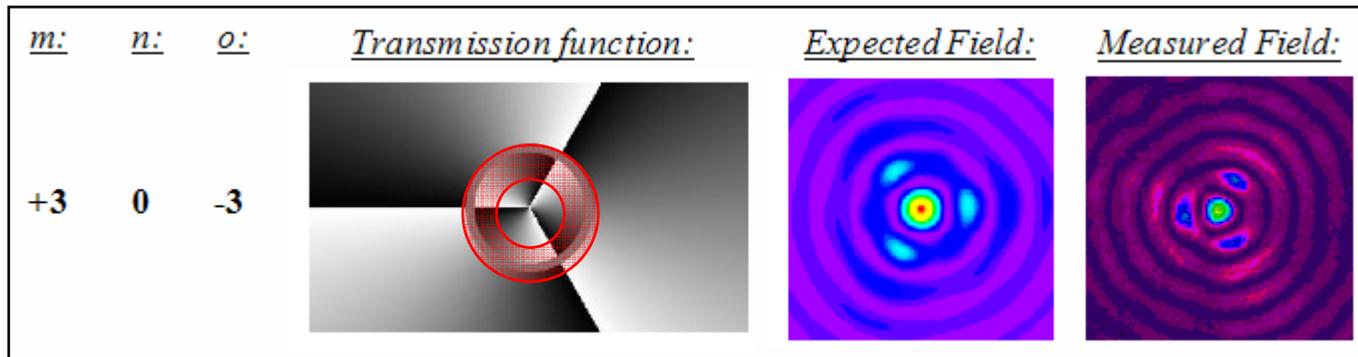
Resulting Field: 
$$A_{m,n}(r, \varphi, z) \propto J_m\left(\frac{k_0 r}{f}\right) + J_n(k_0 r)$$



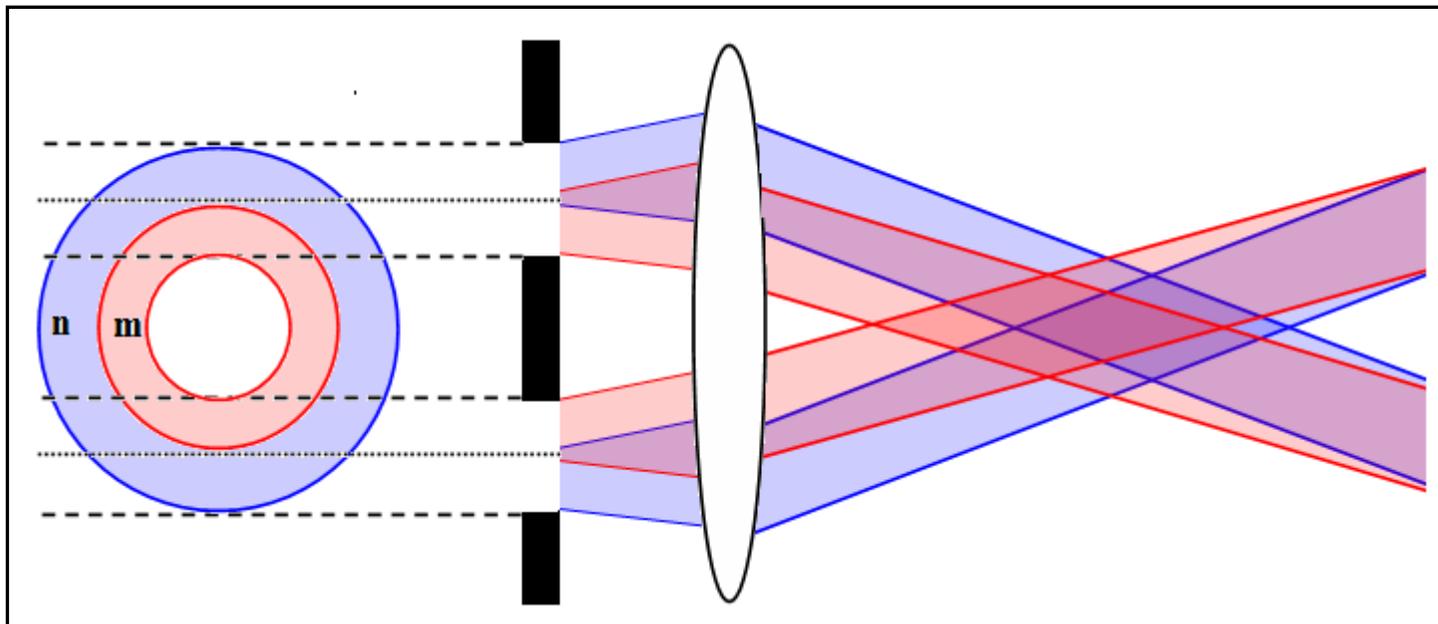
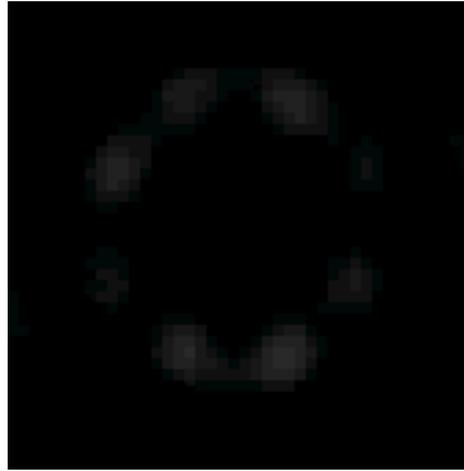
# Experimental Results: Superposition of 3 Bessel Fields

Transmission Function: 
$$\tau(r, \varphi) = \begin{cases} \exp(im\varphi) & (R - \frac{\Delta}{2}) \geq r \geq (R - \Delta) \\ \exp(in\varphi) & (R + \frac{\Delta}{2}) \geq r \geq (R - \frac{\Delta}{2}) \\ \exp(io\varphi) & (R + \Delta) \geq r \geq (R + \frac{\Delta}{2}) \end{cases}$$

Resulting Field: 
$$A_{m,n,o}(r, \varphi, z) \propto J_m\left(\frac{k_0 r}{f}\right) + J_n\left(\frac{k_0 r}{f}\right) + J_o\left(\frac{k_0 r}{f}\right)$$



# Experimental Results: Propagation

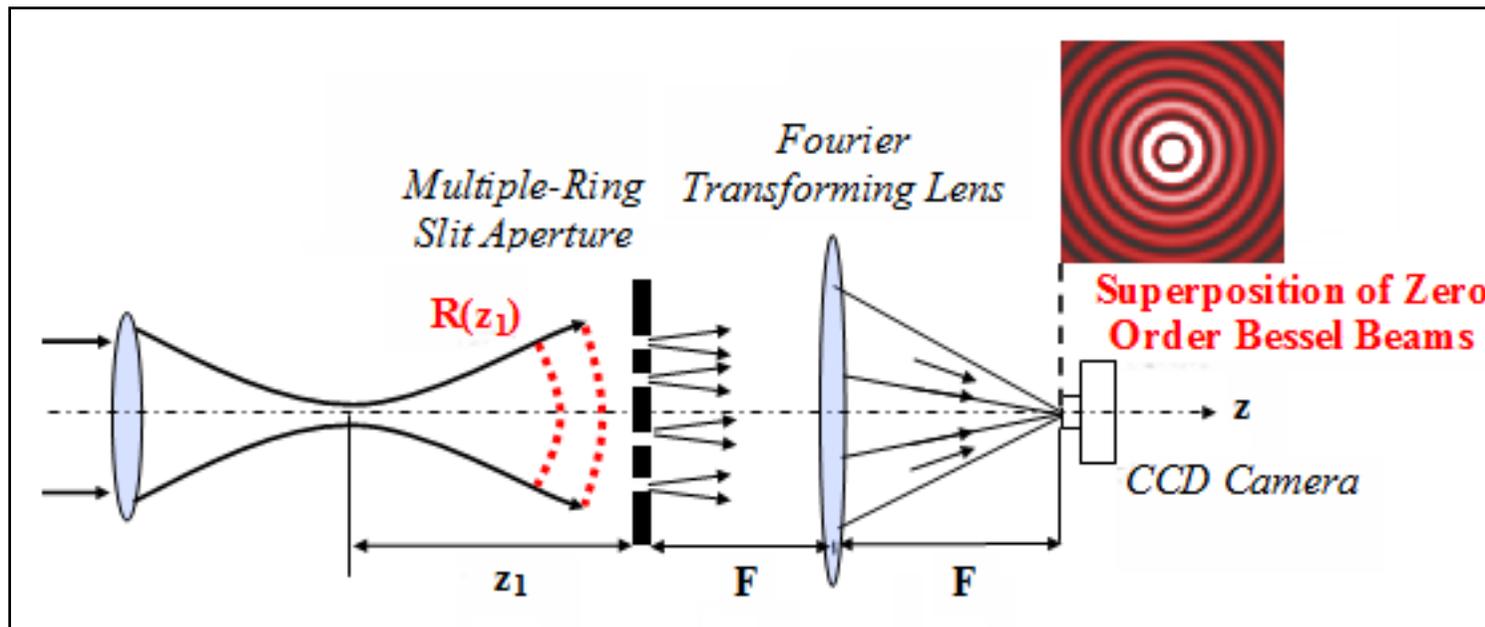




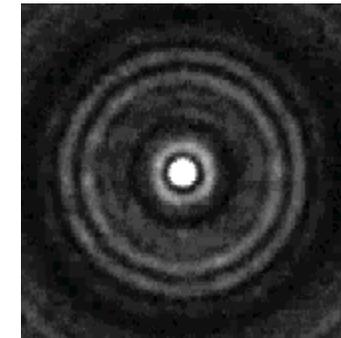
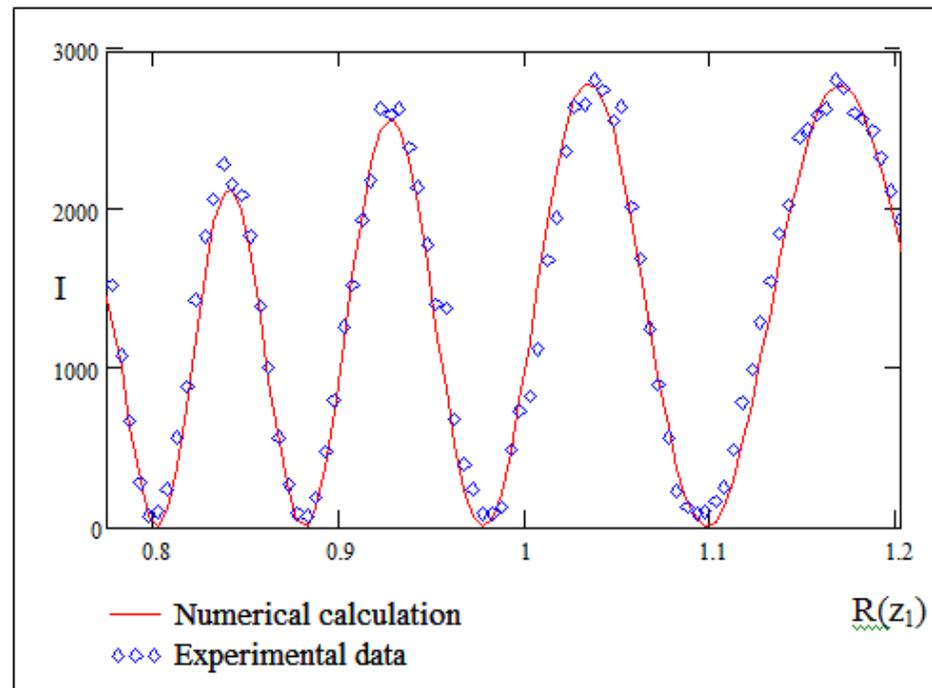
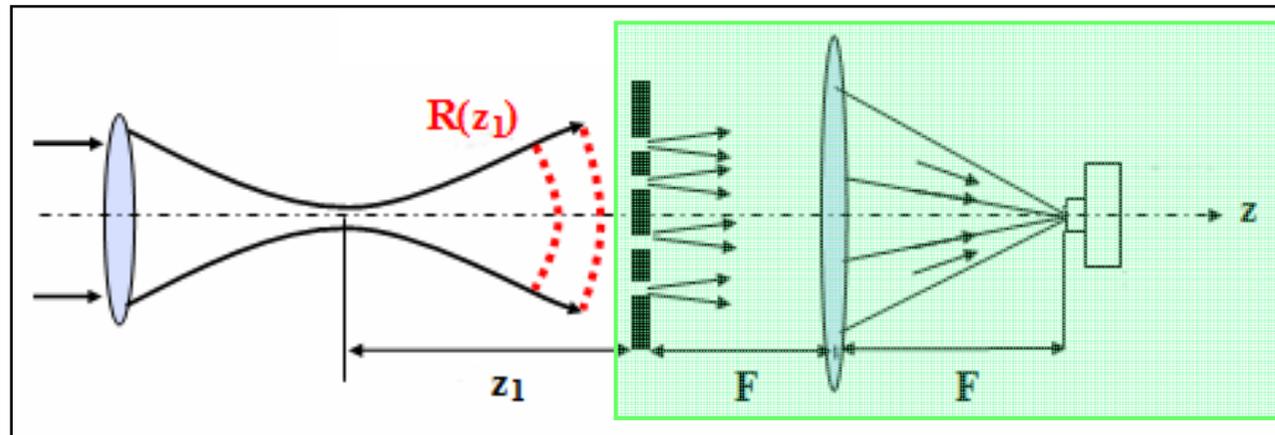
# Application: Characterising the radius of curvature by the use of superimposed Bessel fields

The superposition of zero order Bessel beams can be used to measure the radius of curvature of a reflecting surface.

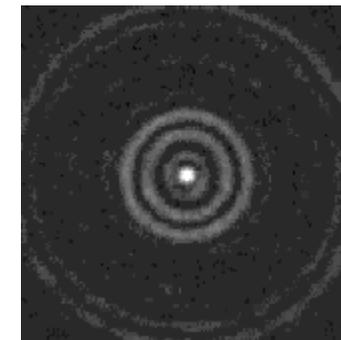
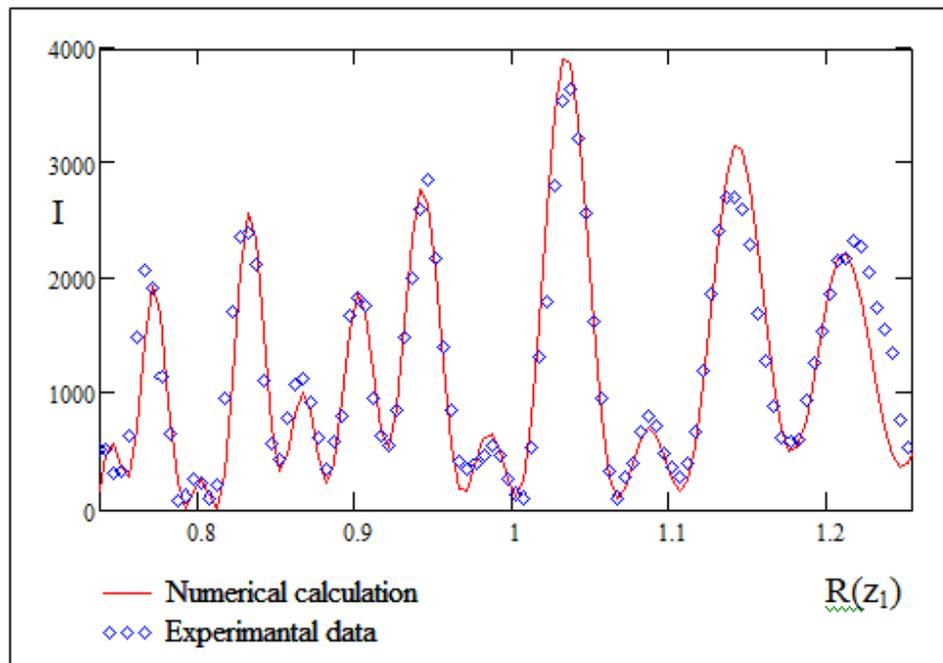
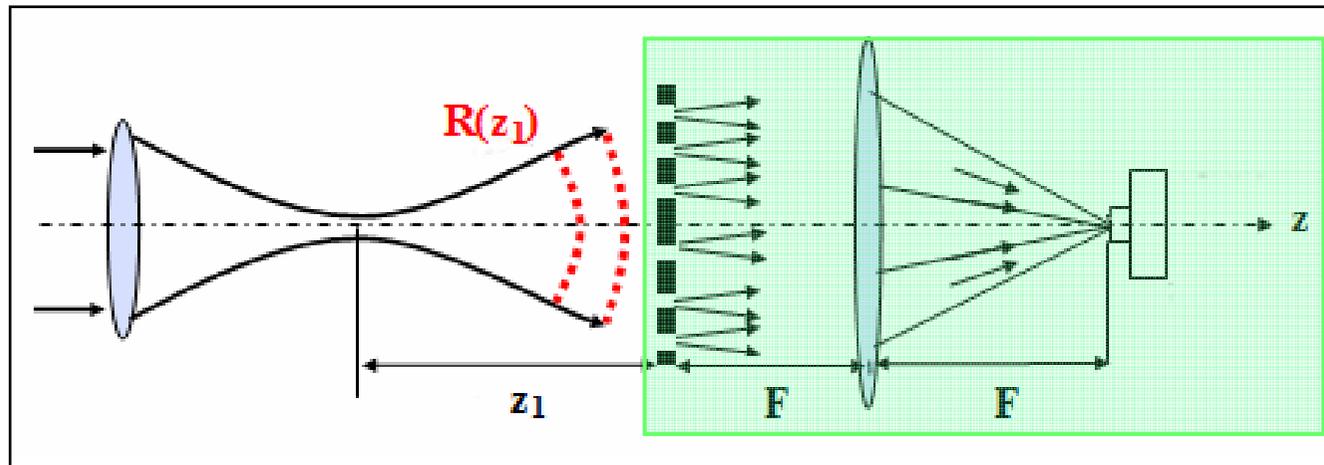
This approach is based on the fact that the intensity distribution of the superimposed Bessel beams is a sensitive function of the relative phases between the constituting beams.



# Experimental Setup and Results: Two superimposed Bessel fields



# Experimental Setup and Results: Three superimposed Bessel fields



**Thank You**

